## Packet #3

This contains extension topics that were added into current Math 2 units. Refer to your text book and notes to review ideas on Probability and Algebra concepts.

These two lessons are add-ons to the	e Math 2 Unit on Prob	bability. Refer to your textbook Ch. 13 Objective 3	i
13.2 Fundamental Counting Principl	e & Permutations	Name	
Solve each problem on a separate pie 1. A band sells t-shirts in 3 sizes and	ece of paper. Show wd 2 different colors. H	work for EVERY problem. How many different t-shirts are there to choose fro	m
<ol> <li>Each player on the baseball team 34". They can also choose either</li> </ol>	can order a bat with n Ash or Maple for the	natural or black finish with lengths of 32", 33", e materials. How many choices are there?	
3. A skier has 2 pairs of skis, 2 pairs another pair of gloves, how many		erent pairs of gloves to choose from. If she buys will be possible?	
Evaluate. Write out the formula for 64. $_6P_3=$	each problem. 5. <sub>8</sub> P <sub>6</sub> =	6. <sub>5</sub> P <sub>5</sub> =	
7. $_{10}P_2=$	8. <sub>7</sub> P <sub>4</sub> =	9. $_{4}P_{1}=$	
Show your work for each problem.  10. How many ways can arrange the	eletters in the word FF	RACTION?	
11. How many distinguishable perm	utations of the letters	s DOCTOR are possible?	
12. How many distinguishable permi	utations of the letters	s HAWAIIAN are possible?	
13. How many different 6-character in next three characters are numbers. Le		ade if the first three characters are letters and the ay repeat.	

14.	Consider	#13	above	if repeats	are	not	allowed
1	Consider	,, 10	uoove	ii repeats	arc	HOU	anowed

- 15. 30 people are running a race. In how many ways can people win first, second, and third place?
- 16. In how many different orders can 6 people sit in a row of 6 seats at a movie theater?
- 17. Explain why you can use n! to find the number of possible orders for n objects.
- 18. The numbers 1-10 are put in a hat. If the numbers are taken out one at a time, what is the probability they come out in ascending order?

13.3 Fundamental Counting Principle & Combinations Evaluate. Write out the formula for each problem.

1. 
$$_{6}C_{3}=$$

2. 
$${}_{8}C_{6}=$$

3. 
$${}_{5}C_{5}=$$

4. 
$${}_{10}C_2 =$$

5. 
$$_{7}C_{4}=$$

6. 
$${}_{4}C_{1}=$$

Tell whether each of the following is a permutation or combination.

- 7. An arrangement of the letters in the word MATH
- 8. Choosing a clean-up committee from the 35 students in the class

9. Determining first, second, and third place in a race.
10. Looking at 14 photos and selecting one for the photobook front cover and one for the back cover.
11. Dialing the numbers in a telephone number.
12. Determining the batting order for the 9 players on a baseball team.
13. The answers on a true-false test.
14. Ordering a dish of ice cream with 2 scoops chosen from 31 flavors.
15. Three books selected from a collection of 20 books.
16. Buying ten items at the grocery store.
Show your work for each combination.  17. A basketball coach chooses 5 players from a group of 8 to start the game. How many different groups of starting players are possible?
18. A smoothie place has ten kinds of fruit. How many different smoothies can be made if each one has four different fruits in it?
19. How many ways can three dancers be selected for a number if 18 dancers tried out?
20. A committee is made up 6 members: 3 boys and 3 girls. If 6 boys and 5 girls want to be on the committee, how many different committees are possible?

21. A dodgeball tournament requires teams of 4 students and 2 teachers. If 10 students and 3 teachers agree to play, how many ways can a team be picked?
Work out the following problems. Some are combinations and some are permutations.  22. AP students are given a list of 9 books for summer reading. How many ways can 5 books be selected from the list?
23. Quality control for the Sharpie Company tests 2 out of 150 pens. In how many ways can those two pens be selected?
24. One hundred students qualified to run finals at Woodward Park. In how many ways can 1 <sup>st</sup> , 2 <sup>nd</sup> , and 3 <sup>rd</sup> be awarded?
25. A teacher, her aide, and 5 students are lining up. How many different ways can they line up if the teacher must be in the front of the line and the aide must be in the back?
26. John goes to the store to buy ketchup, mustard, mayonnaise, BBQ sauce, tomatoes, and lettuce. He realizes he only has enough money to buy 3 of the items. How many groups of 3 items are possible?
27. The freshmen council has 10 members. In how many ways can they select a President, a Vice President, a Secretary, and a Treasurer?
28. A tablet has comes in 32 GB, 64 GB, and 128 GB sizes with color options black, white, red, and blue. It also comes with or without cellular data capabilities. How many unique tablets are possible?
29. How many distinguishable permutations of the letters NEEDED are possible?
Find the probability for the scenario.  30. A game involves correctly choosing the correct 5 randomly drawn numbers out of 1-18. What is the chance of winning?

Algebra Review

Factor completely: 1.  $m^2 - 9n^2$ 

2. 
$$x^2 + 8x + 15$$

3. 
$$36-49m^2$$

4. 
$$2x^2 - 72$$

5. 
$$x^{\frac{1}{2}} + 5x^{\frac{1}{4}} + 6$$

6. 
$$10 - 3x - x^2$$

7. 
$$5x^3 - 125xy^2$$

8. 
$$6x^2 + 5x + 1$$

9. 
$$16 - m^4$$

10. 
$$3x^{\frac{2}{3}} - 8x^{\frac{1}{3}} - 3$$

11. 
$$9a^4 - 13a^2 + 4$$

12. 
$$a^2 + 2ab + b^2$$

13. 
$$x(a+b) + y(a+b)$$

14. 
$$3(a+b)+(4-x)(a+b)$$
 15.  $(x+y)^2-a^2$ 

15. 
$$(x+y)^2 - a^2$$

16. 
$$4(m+n)^2 - 81$$

$$18.(x + y)^2 - 3(x + y) + 2$$

19. 
$$(xy+2z)^2-9x^2y^2$$

$$20.(x^2-3x-6)^2+10(x^2-3x-6)+16$$

## Factor Completely:

1. 
$$ac + bc - ad - bd$$

2. 
$$3ab + 4cd - cb - 12ad$$
 3.  $2st - 3t - 4s + 6$ 

3. 
$$2st - 3t - 4s + 6$$

4. 
$$x^2 - 10x + 25 - y^2$$

5. 
$$v^2 - x^2 - 2x - 1$$

4. 
$$x^2 - 10x + 25 - y^2$$
 5.  $y^2 - x^2 - 2x - 1$  6.  $x^2y^2 - 4y^2 + 5x^2 - 20$ 

7. 
$$x^2y^2 - x^2 - 9y^2 + 9$$

7. 
$$x^2y^2 - x^2 - 9y^2 + 9$$
 8.  $4cd + 8d^2 - 8cf - 16df$  9.  $a^3 + b^3$ 

9. 
$$a^3 + b^2$$

10. 
$$a^3 + 3a^2b + 3ab^2 + b^3$$
 11.  $a^9 + 1$ 

11. 
$$a^9 + 1$$

12. 
$$125a^6 - b^3$$

13. 
$$64a^3 - 8b^3$$

14. 
$$(3x+1)^3 - (2x)^3$$

14. 
$$(3x+1)^3 - (2x)^3$$
 15.  $(x+y)^3 - (x-y)^3$ 

Simplify the following.

$$1. \ \frac{x^2 - 4}{x^3 + 4x^2 + 4x}$$

$$2. \ \frac{x^3 + 1}{(x+1)^3}$$

$$3. \ \frac{x^4 - 16}{x^3 - 2x^2 + 4x - 8}$$

$$4. \ \frac{9-h^2}{12-h-h^2}$$

$$5. \quad \frac{\left(x+h\right)^2-h^2}{x}$$

Simplify the following.

1. 
$$\frac{\frac{1}{a}}{\frac{2}{3a}}$$

$$2. \quad \frac{\frac{1}{2} + \frac{1}{a}}{\frac{1}{2a}}$$

$$3. \qquad \frac{\frac{x}{2} - \frac{y}{3}}{\frac{1}{4}}$$

$$4. \quad \frac{\frac{1}{x} + \frac{1}{a}}{\frac{1}{a} + \frac{2}{x}}$$

$$5. \quad \frac{a + \frac{a}{b}}{-b + \frac{1}{b}}$$

$$6. \quad \frac{\frac{x}{y} - \frac{y}{x}}{\frac{1}{x} - \frac{1}{y}}$$

7. 
$$\frac{\frac{a+b}{a-b} - \frac{a-b}{a+b}}{\frac{b}{a-b} + \frac{a}{a+b}}$$

$$8. \qquad \frac{\frac{1}{x^2} - \frac{1}{4}}{x - 2}$$

$$9. \qquad \frac{\frac{x}{x-2} - 2}{x-4}$$

10. 
$$\frac{\frac{1}{x-1} - \frac{8}{x^2 - 1}}{\frac{2}{x+1} - \frac{1}{x-1}}$$