

Multiplying and dividing rational expressions use the same properties used to multiply and divide numerical fractions. If  $a$ ,  $b$ ,  $c$ , and  $d$  represent polynomials (where  $b \neq 0$  and  $d \neq 0$ ), then  $\frac{a}{b} \cdot \frac{c}{d} = \frac{ac}{bd}$ .

[1-4] What is the product?

$$1. \frac{4x+8}{6x-10} \cdot \frac{15-9x}{x^2+6x+8}$$

Steps

1. Completely factor the numerator and denominator (if possible)
  - \*gcf factoring
  - \*trinomial factoring
  - \*difference of squares
2. Rewrite as a single fraction
3. Divide out the common or opposite factor(s).

$$2. \frac{3x^2}{x+2} \cdot \frac{x^2+3x+2}{x}$$

$$3. \frac{4x^2}{3xy} \cdot \frac{x^2y^3}{6xy}$$

$$4. \frac{x^2y}{5x} \cdot \frac{15x^3y^2}{2x^2y^4}$$

$$5. \frac{x^3-8}{4-x^2} \cdot \frac{x^2+5x+6}{x^2+3x}$$

Recall that  $\frac{a}{b} \div \frac{c}{d} = \frac{a}{b} \cdot \frac{d}{c}$ , where  $b \neq 0$ ,  $c \neq 0$  and  $d \neq 0$ . When you divide rational expressions, first rewrite the quotient as a product using the reciprocal before dividing out common factors.

[1-4] What is the quotient?

$$1. \frac{x^2-25}{4x+28} \div \frac{x-5}{x^2+9x+14}$$

$$2. \frac{y+4}{y^2+5y+6} \div \frac{3y^2+12y}{2y^2+5y-3}$$

$$4. \frac{y^2+6x+8}{y^2+y-2} \div \frac{y+4}{2y+4}$$

Steps

1. Completely factor the numerator and denominator (if possible)
  - \*gcf factoring
  - \*trinomial factoring
  - \*difference of squares
2. To divide by a rational expression, multiply by its reciprocal.
3. Rewrite as a single fraction
4. Divide out the common or opposite factor(s).

$$3. \frac{x^2}{3xy} \div \frac{x^2y^2}{6xy}$$

$$5. \frac{\frac{x^2+x-12}{x^2+4x}}{\frac{6-2x}{x^2+x}}$$